#### ARTICLE

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# Hydrodynamic effects in fast AFM single-molecule force measurements

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Abstract Atomic force microscopy (AFM) allows the critical forces that unfold single proteins and rupture individual receptor-ligand bonds to be measured. To derive the shape of the energy landscape, the dynamic strength of the system is probed at different force loading rates. This is usually achieved by varying the pulling speed between a few nm/s and a few µm/s, although for a more complete investigation of the kinetic properties higher speeds are desirable. Above 10 µm/s, the hydrodynamic drag force acting on the AFM cantilever reaches the same order of magnitude as the molecular forces. This has limited the maximum pulling speed in AFM single-molecule force spectroscopy experiments. Here, we present an approach for considering these hydrodynamic effects, thereby allowing a correct evaluation of AFM force measurements recorded over an extended range of pulling speeds (and thus loading rates). To support and illustrate our theoretical considerations, we experimentally evaluated the mechanical unfolding of a multi-domain protein recorded at 30 µm/s pulling speed.

**Keywords** Atomic force microscopy · Loading rates · Drag force · Dynamic force spectroscopy · Ig27-8

**Abbrevations** AFM: atomic force microscopy · pN: piconewton · BR: bacteriorhodopsin · DFS: dynamic force spectroscopy · Ig27: immunoglobulin 27 · If27-8: immunoglobulin 27 octameric construct · BFP: biomembrane force probe

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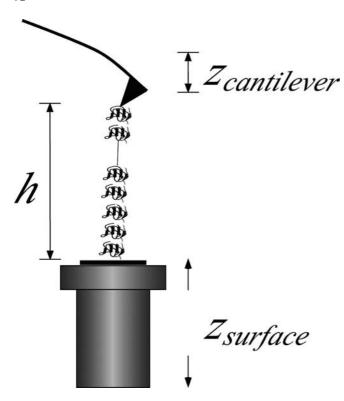
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## Introduction

Since its invention by Binnig, Quate and Gerber in 1986, the atomic force microscope has proven to be an excellent tool for imaging a wide class of biological samples such as cells, nucleic acids and proteins (Czajkowsky et al. 2000; Müller et al. 2002a). More recently, the micromachined cantilever of the AFM has been employed to measure the forces that stabilize single proteins and form molecular bonds at the piconewton (pN) scale (Lee et al. 1994; Moy et al. 1994; Rief et al. 1997, 1998; Fritz et al. 1998). To this end, a single protein or ligand-receptor pair is tethered between the tip of the cantilever and a supporting sample surface (Fig. 1). The tip-sample separation is then continuously increased by displacing the surface at constant speed with a piezoelectric actuator. Plotting force (as derived by the deflection of the cantilever and Hooke's law) against the tip-surface separation then yields a force-extension spectrum that is characteristic of the molecule being studied.

In their initial experiments, Rief and coworkers applied single-molecule force spectroscopy to the muscle protein titin, which consists of repeats of globular immunoglobulin and tenascin domains (Rief et al. 1997, 1998). The continuous extension of the protein resulted in the subsequent unfolding of the globular domains, while the force necessary for the unfolding of each domain was revealed from the force spectrum. In contrast to most other unfolding experiments on globular proteins, the combination of single-molecule imaging and force spectroscopy yielded surprisingly detailed insight into inter- and intramolecular interactions of the membrane protein bacteriorhodopsin (BR) (Oesterhelt et al. 2000). It has been shown that structural elements of BR unfold sequentially and that their stability depends on the physiological environment of the protein (Müller et al. 2002b; Janovjak et al. 2003).

Recently, dynamic force spectroscopy (DFS) experiments have provided insights into the energy landscapes



**Fig. 1** Single-molecule force measurement on a multi-domain protein. A single multimeric protein construct consisting of several Ig27 domains is tethered between the AFM cantilever and a sample surface. Continuously increasing the tip–surface separation (h) by retracting the surface by  $z_{\rm surface}$  leads to unfolding of the individual domains. Measuring the deflection of the cantilever ( $z_{\rm cantilever}$ ) allows the force applied to the protein and thus required to unfold the single domains to be derived (Fig. 3)

underlying the mechanical properties of single biological molecules (Strunz et al. 1999; Evans 2001; Williams et al. 2003). In DFS, unfolding or unbinding forces are measured at various pulling speeds. Monitoring the most probable unbinding force as a function of pulling speed allows the width of potential barriers crossed during the unfolding process and the natural transition rates over these barriers to be revealed (Evans and Ritchie 1997; Evans 2001). In the case of Ig27 domains and single transmembrane helices of BR, it was found that a  $\approx$ 4-Å extension triggers unfolding across a single potential barrier (Rief et al. 1997; Williams et al. 2003; Janovjak et al. 2004). Merkel and coworkers demonstrated that during unbinding of biotin from (strept-)avidin several potential barriers are crossed. Their positions along the separation distance could be localized using DFS without comparable spatial resolution of the instrument (Merkel et al. 1999).

All recent DFS experiments with AFM had in common that the pulling speeds were varied in the range from a few nm/s to  $\approx\!10~\mu\text{m/s}$  (de Paris et al. 2000; Williams et al. 2003). However, to obtain a more complete picture of their kinetic properties, it would be desirable to investigate the systems over an increased range of pulling speeds (Lo et al. 2001). At speeds greater than  $\approx\!10~\mu\text{m/s}$ , the speed-dependent hydrody-

namic drag force acting on the cantilever is of the same magnitude as the peak forces measured on single biological molecules. As the tip velocity is not constant during typical measurements, large deviations in the forces are obtained if the hydrodynamic effects are not considered. This effect appears most significant at pulling speeds above a few  $\mu m/s$ . Here, we combined hydrodynamic force measurements and theoretical considerations to provide a method for the correct evaluation of force measurements recorded at pulling speeds, and hence loading rates, up to two orders of magnitude higher than previously possible.

#### **Materials and methods**

Atomic force microscopy

A commercial atomic force microscope (AFM) optimized for force measurements (MultiMode PicoForce, Veeco Metrology, Santa Barbara, CA) was equipped with a *x-y-z*-piezo scanner with a sensored and closed-loop 20- $\mu$ m *z*-axis. The spring constants of the two silicon nitride cantilevers (small V-shaped lever: Olympus OTR4, k=0.095 N/m, length (l)=100  $\mu$ m, width (w)=18  $\mu$ m, thickness (t)=0.4  $\mu$ m; large V-shaped lever: ThermoMicroscope MSCT-AUNM Microlever C, k=0.015 N/m, l=320  $\mu$ m, w=22  $\mu$ m, t=0.6  $\mu$ m; Veeco Metrology) were calibrated in liquid using thermal fluctuation analysis (Butt and Jaschke 1995; Florin et al. 1995).

Experimental unfolding data on Ig27-8

Individual molecules were unfolded as recently described (Rief et al. 1997) using the large V-shaped lever in PBS (Sigma) after adsorption to a freshly prepared gold surface. We used the worm-like chain model with a persistence length of 4 Å and a monomer length of 3.6 Å to describe the force–extension relationship of unfolded parts of the protein in the force spectrum (Rief et al. 1997).

#### **Results and discussion**

Hydrodynamic drag force acting on an AFM cantilever

Like any other object moved through a solution, the AFM cantilever experiences a hydrodynamic drag force due to viscous friction with the surrounding liquid (Walters et al. 1996; Gittes and Schmidt 1998; Viani et al. 1999a). Drag forces have been previously quantified for spheres as well as for an AFM cantilever close to a surface (Cox and Brenner 1967; Alcaraz et al. 2002). For a cantilever, it has been suggested that the dimensions of the lever and the distance to the surface be scaled by introducing two empirical coefficients (Roters and Johannsmann 1996; O'Shea and Welland

1998; Alcaraz et al. 2002). As recently proposed, the drag force ( $F_d$ ) acting on the cantilever can then be described as:

$$F_{\rm d} = \frac{6 \pi \eta a_{\rm eff}^2}{h + d_{\rm eff}} \cdot v_{\rm tip} \tag{1}$$

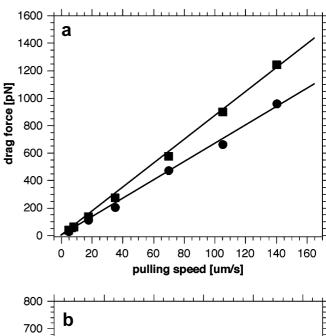
where  $\eta$  is the viscosity of the liquid, h the tip-surface separation and  $v_{\text{tip}}$  denotes the tip velocity (Alcaraz et al. 2002). The empirical coefficients  $a_{\text{eff}}$  and  $d_{\text{eff}}$  represent the effective size of the cantilever and the effective cantilever tip height respectively. Equation (1) is valid in regimes of purely viscous flow, i.e. where the Reynolds number ( $Re = a_{\text{eff}} v_{\text{tip}} \rho / \eta$ ) is below 1 (Alcaraz et al. 2002). For a typical measurement in water at room temperature  $(\eta = 1 \text{ mNs/m}^2, \text{ density } \rho = 1 \text{ g/cm}^3), Re \text{ is well below } 1$ for pulling speeds as high as a few mm/s. We quantified the hydrodynamic drag force as a function of the pulling speed and tip-sample separation for two V-shaped cantilevers. Figure 2a shows the linear dependence of the drag force on the pulling speed, and Fig. 2b the more complex dependence on the tip-surface separation. As predicted, an increase in the drag force is observed close to the surface (Roters and Johannsmann 1996). Consequently,  $a_{\text{eff}}$  and  $d_{\text{eff}}$  were determined by measuring the drag force at a fixed speed for different tip-sample separations and fitting the data to Eq. (1). For  $a_{\text{eff}}$  we obtained  $35.13 \pm 0.07$  µm (small lever) and  $52.06 \pm 0.08$  µm (large lever), and for  $d_{\rm eff}$  3.70  $\pm$  0.18  $\mu m$  (small lever) and  $5.48 \pm 0.17$  µm (large lever). Although the above model predicts  $F_d = 0$  for large separations (Alcaraz et al. 2002), it accurately describes the drag force for a range of tipsample separations sufficient for single-molecule force measurements  $(0-2.5 \mu m, Fig. 2b)$ .

# Correcting AFM force measurements for hydrodynamic effects

The hydrodynamic force has to be considered in force measurements with pulling speeds above a few µm/s as it reaches the same magnitude (Fig. 2a) as the forces measured on single molecules (Lee et al. 1994; Moy et al. 1994; Rief et al. 1997, 1998; Fritz et al. 1998). Including a correction factor for the hydrodynamic drag is complicated by the fact that the tip velocity is not constant during a typical measurement. Bending of the cantilever towards the surface is observed in most experiments when the cantilever is connected to the surface via a flexible linker molecule (e.g. polymer spacers for the study of single ligand-receptor pairs or already unfolded domains in case of proteins) (Rief et al. 1997; Hinterdorfer et al. 2000). Thus a direct consequence of any adhesive event is that the tip velocity decreases. In these cases, the tip-surface separation can be written as:

$$h = z_{\text{surface}} - z_{\text{cantilever}} \tag{2}$$

where  $z_{\text{surface}}$  is the distance the surface has moved, and  $z_{\text{cantilever}}$  is the cantilever deflection (Fig. 1). The tip



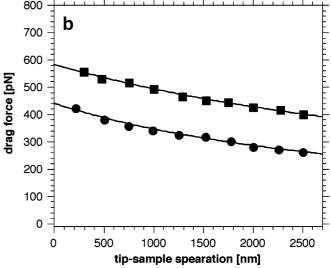


Fig. 2a, b Hydrodynamic drag force acting on an AFM cantilever. Force measurements with AFM cantilevers are subject to hydrodynamic drag forces, which depend on the pulling speed and tip—sample separation. a Linear dependence of the drag force on the pulling speed recorded at a distance of 500 nm from the surface. Slopes of the linear fits are  $8.68 \pm 0.11$  pN s/µm (squares, large lever in PBS) and  $6.67 \pm 0.11$  pN s/µm (circles, small lever in water). b Non-linear dependence of drag force on the tip–sample separation (recorded at  $70 \mu \text{m/s}$ ) which allows the empirical drag coefficients  $a_{\text{eff}}$  and  $d_{\text{eff}}$  to be determined according to Eq. (1) (solid lines). SDs are of comparable size with the markers

velocity can then be calculated by taking the derivative of the tip-sample separation with respect to time for each point of the curve:

$$v_{\rm tip} = \frac{dh}{dt} \tag{3}$$

As the tip velocity decreases during the measurement, the hydrodynamic drag force acting on the cantilever will also decrease. Therefore, the real force applied to the molecule is underestimated (i.e. it is larger than the measured force) if hydrodynamic effects are not considered. This additional hidden force ( $\Delta F$ ) can be written as

$$\Delta F = F_{\rm d}(v, h) - F_{\rm d}(v_{\rm tip}, h) \tag{4}$$

It is equal to the difference between the drag force calculated for the constant speed of the surface,  $F_{\rm d}(\nu,h)$ , and the drag force calculated by taking the tip velocity at each point of the curve into account,  $F_{\rm d}(\nu_{\rm tip},h)$ . Accordingly, the net force  $(F_{\rm net})$  acting on the molecule is:

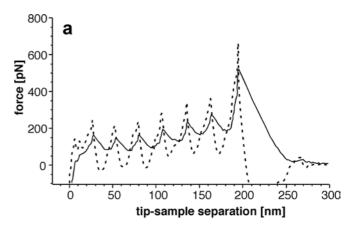
$$F_{\text{net}} = F_{\text{measured}} + \Delta F \tag{5}$$

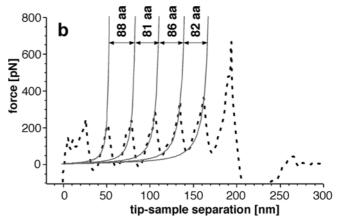
where  $F_{\rm measured}$  is the measured force data. Equation (5) is valid if the offset of the unprocessed data is corrected by moving the non-contact part of the curve to zero force.

#### Unfolding a multi-domain protein at 30 µm/s

We observed the predicted underestimation during the unfolding of an octameric immunoglobulin-27 protein construct (Ig27-8) at 29.7  $\mu$ m/s (Fig. 3a, solid line). The continuous extension of the multi-domain protein led to sequential unfolding of the domains, and thus the curve shows the characteristic sawtooth pattern (Rief et al. 1997; Fig. 3a, solid line). We measured an average unfolding force of  $207.8 \pm 35$  pN (n = 25) for the unfolding of single Ig27 domains. However a force of  $\approx 250$  pN would be expected at this pulling speed when one extends the experimentally determined speed dependence of the unfolding forces to 30  $\mu$ m/s (Williams et al. 2003).

To attribute this disagreement to the hydrodynamic effect described above, we inspected the tip-sample separation (Fig. 4a) and the tip velocity (Fig. 4b) in the course of the measurement. The tip-sample separation was derived according to Eq. (2), and each of the seven force peaks led to a local deviation from the linear behavior (Fig. 4a, arrows). Remarkably, the tip velocity (Fig. 4b, solid line) was not constant during the force curve and differed significantly from the speed with which the surface was separated from the cantilever (Fig. 4b, dashed line). As mentioned above, the tip moved more slowly when the cantilever was bent towards the surface. From the tip velocity we calculated the hydrodynamic drag force acting on the cantilever according to Eq. (1) (Fig. 4c). The observed decrease in the drag force indicates that the molecule was subjected to a hidden force in addition to the measured force. The re-evaluation of the curve following Eq. (5) is shown in Fig. 3, where the dashed line corresponds to the corrected force trace. It becomes clear that consideration of the hydrodynamic drag increases the peak forces significantly. After the correction, the measured unfolding force of a single Ig27 domain was  $274.7 \pm 37.5 \text{ pN}$ (n=25). As this value lies within the expected range it is suggested that correcting for the hydrodynamic drag





**Fig. 3a, b** Unfolding the multi-domain protein at 30 μm/s. **a** Plotting force as a function of tip-sample separation during the unfolding of the protein construct as shown in Fig. 1 yields the force extension curve (*solid line*). The sequential unfolding of the domains results in the characteristic sawtooth pattern. The *dashed line* corresponds to the same force trace after consideration of the hydrodynamic drag force. A significant increase in the peak forces by  $\approx 50\%$  is observed. **b** Fitting the corrected force trace with the WLC model indicates good agreement between the corrected experimental data and the expected extension pattern. The number of amino acid residues (*aa*) determined for each domain is given in the figure and is close to the length of the Ig27 domain (89 aa)

allows a more correct evaluation of the measurement obtained at 29.7  $\mu$ m/s.

#### Factors limiting AFM pulling speeds

The apparent maximum instrumental pulling speed in AFM single-molecule force measurements is a few hundred  $\mu m/s$  (Lo et al. 2001). However, even after considering hydrodynamic contributions, the resonance frequency of the cantilever and its viscoelastic response time still limit AFM force measurements to lower pulling speeds. To ensure a proper response of the cantilever, the frequency of any repetitive feature in the force spectrum should be significantly lower than the resonance frequency of the cantilever (Viani et al. 1999a). When pulling Ig27-8 with a cantilever of 7-kHz resonance frequency (e.g. the small V-shaped lever), a speed of  $\approx 100~\mu m/s$  is the limit, as this corresponds to

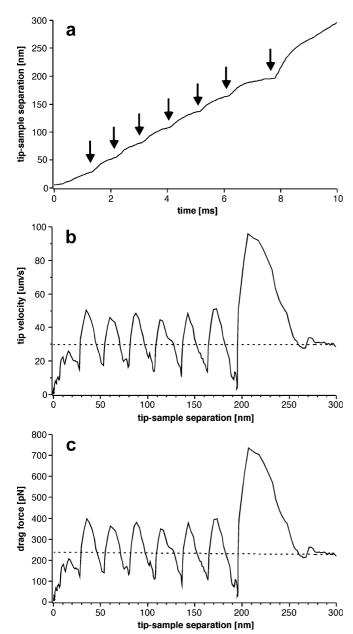


Fig. 4a–c Tip velocity and hydrodynamic drag force. a The separation of tip and sample during the measurement shown in Fig. 3a was derived following Eq. (2). A ridge in the linear curve is observed where the cantilever interacts with the surface (arrows). b The tip–sample separation was derived with respect to time according to Eq. (3) to obtain the velocity of the tip for each point of the force curve. As expected the tip moves more slowly when the cantilever interacts with the surface. c The hydrodynamic drag force acting on the tip of the cantilever was calculated for each point of the curve according to Eq. (1). The dashed line indicates the drag force for an untethered cantilever

a peak frequency in the force spectrum of  $\approx 3$  kHz. The viscoelastic response time of the cantilever is determined by the force probe's damping (Evans 2001). Assuming a probe damping ( $\zeta$ ) on the order of  $10^{-3}$  pN s/nm and a spring constant (k) of 100 pN/nm, the time scale of viscoelastic responses ( $t = \zeta/k$ ) lies

in the range of  $10^{-5}$  s (Evans 2001). This corresponds to a 'response frequency' of 100 kHz and thus to  $\approx 30$  responses per unfolding peak when unfolding Ig27-8 at  $100~\mu m/s$ .

## Comparison with ultra-small cantilevers

Such fast-pulling experiments could previously only be conducted with the help of ultra-small cantilevers (Viani et al. 1999a). Ultra-small cantilevers are typically  $\approx$ 10–14 µm long, 3–5 µm wide and 100 nm thick (Viani et al. 1999b). The reduced cantilever size and mass result in smaller drag coefficients and higher resonance frequencies and thus allow access to higher pulling speeds. However, the use of such small cantilevers requires special instrumentation with a smaller laser spot size (Viani et al. 1999b). Furthermore, the production and handling of small cantilevers are challenging because, in order to obtain the same spring constant, the cantilever needs to be thinner than standard-size cantilevers (Viani et al. 1999a). It is important to note that our correction procedure is also suitable for extending the pulling speed range of small cantilevers.

# Comparison with other force probe methods

Although many methods are in use, the AFM and the biomembrane force probe (BFP) may comprise the most frequently used techniques for measuring forces at a single-molecule level. The approach presented here allows a more complete investigation of the kinetic properties of the single molecule by AFM, as the range of accessible loading rates is extended. An extension becomes especially important because force measurements performed with the BFP are limited to loading rates of  $\approx 10^5$  pN/s. This was estimated based on a maximum spring constant of 3 pN/nm and retraction speed of 20 µm/s (Merkel et al. 1999; Evans 2001). Faster retraction speeds may be difficult to achieve due to the temporal resolution of the optical detection systems and hydrodynamic contributions. As a loading rate of 10<sup>5</sup> pN/s corresponds to a pulling speed of 10 μm/s in AFM experiments (assuming a linker stiffness of 10 pN/nm) loading rates one to two orders of magnitude higher than with the BFP now become accessible with AFM.

#### **Concluding remarks**

In this article, we have shown that the tip velocity significantly decreases when an AFM cantilever interacts with a surface via a polymeric linker (Fig. 4b). To avoid an underestimation of the forces applied to the studied interaction, the hydrodynamic force acting on the cantilever has to be considered in measurements recorded at pulling speeds greater than a few  $\mu m/s$  (Fig. 3a). The

approach presented here allows an estimation of the hydrodynamic contributions and therefore extends the range of pulling speeds for all types of cantilevers used in AFM force measurements. This allows a more complete investigation of the kinetic properties as the dynamic range of bond strengths probed is currently limited primarily by the pulling speed.

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